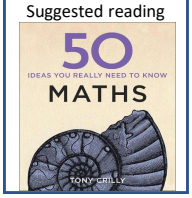
Waingels Maths

Year 9 – Reasoning with Geometry
Deduction

Suggested reading



Want to know more? Scan the QR code to visit the curriculum overview for Year 9 Maths, including topic summaries, key words, and books that you may want to read in your own time

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What do I need to be able to do?

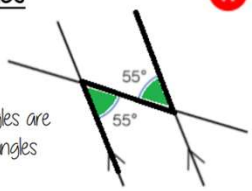
By the end of this unit you should be able to:

- Identify angles in parallel lines
- Solve angle problems
- Make conjectures with angles
- Make conjectures with shapes

Keywords

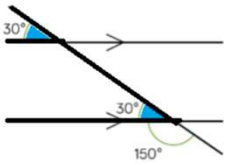
Parallel: two straight lines that never meet with the same gradient
Perpendicular: two straight lines that meet at 90°
Transversal: a line that crosses at least two other lines
Sum: the result of adding two or more numbers
Conjecture: a statement that might be true but is not proven
Equation: a statement that says two things are equal
Polygon: a 2D shape made from straight edges
Counterexample: an example that disproves a statement

Alternate angles (R)



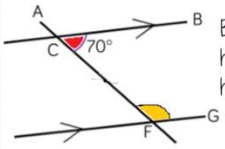
Because alternate angles are equal the highlighted angles are the same size

Corresponding angles (R)



Because corresponding angles are equal the highlighted angles are the same size

Co-interior angles (R)



Because co-interior angles have a sum of 180° the highlighted angle is 110°

As angles on a line add up to 180° co-interior angles can also be calculated from applying alternate/ corresponding rules first

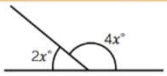
Solving angle problems

Angles on a straight Line
180°

Vertically opposite angles
Equal

Angles around a point
360°

Link angle facts to algebra



Form an equation

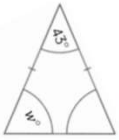
$$2x + 4x = 180°$$

State the reason

The sum of angles on a straight line is 180°

Solve

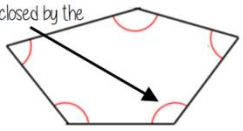
$$2x + 4x = 180°$$
$$6x = 180°$$
$$x = 30°$$



Triangles
Sum of angles is 180°

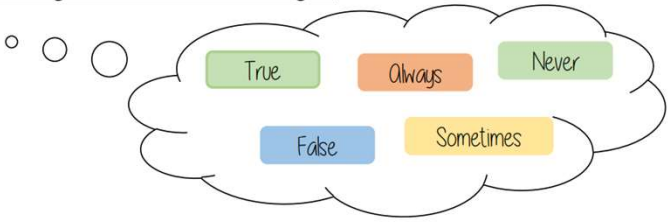
Isosceles have the same base angles

Interior Angles
The angles enclosed by the polygon



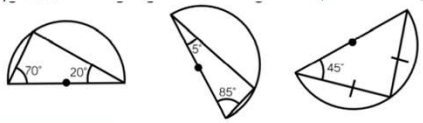
(number of sides – 2) x 180

Making conjectures with angles



Proving a conjecture
A pattern is noticed for many cases

Disproving a conjecture
Only one counterexample is needed to disprove a conjecture



Apply the angle rules
The sum of angles in a triangle is 180°

Test the theory

$$180 - 70 - 20 = 90$$
$$180 - 85 - 5 = 90$$
$$180 - 45 - 45 = 90$$

Make conjecture
The angle that meets the circumference in a semi circle is 90°

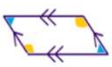
Making conjectures with shapes

Keywords and facts to recall with shape

Area: the amount of space inside a shape
Perimeter: the length around a shape
Regular Polygons: All sides and angles are equal

Quadrilateral Facts

Square
All sides equal size
All angles 90°
Opposite sides are parallel



Parallelogram
Opposite sides are parallel
Opposite angles are equal
Co-interior angles

Rectangle
All angles 90°
Opposite sides are parallel

Rhombus
All sides equal size
Opposite angles are equal

Kite
No parallel lines
Equal lengths on top sides
Equal lengths on bottom sides
One pair of equal angles